

Timing & Freq. Synchronization in OFDM (OFDMA)

Example: $\text{①} \leftarrow \Delta f_{\text{sub}} = 10 \text{ kHz}$; Design Parameter

Bandwidth $\rightarrow N \Delta f_{\text{sub}}$; $N = 2^k \rightarrow$ FFT based ; mod/demod

(Apparent) $N = 1024$; $\Rightarrow \text{BW} = 10.24 \text{ MHz}$; with max

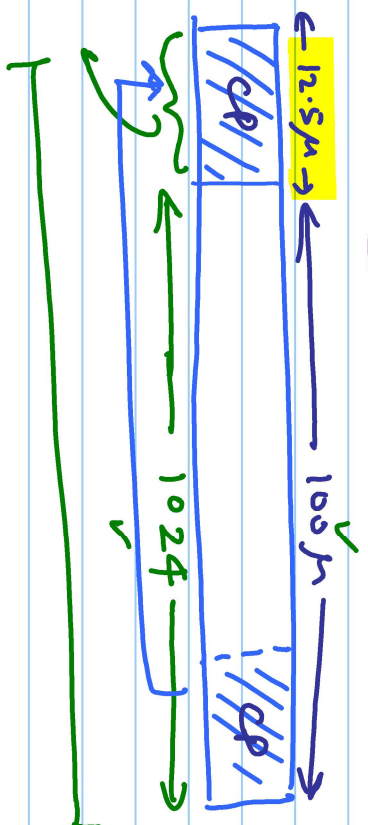
(*) Rx complexity $\propto N$; $10 \text{ MHz} \rightarrow 1024 \rightarrow C$; $20 \text{ MHz} \rightarrow 2048 \rightarrow 2C$

Useful symbol Duration $T_u = \frac{1}{\Delta f_{\text{sub}}} = 100 \mu\text{sec}$;

(*) Cyclic Prefix length $T_{cp} = \frac{1}{8} \cdot T_u = 12.5 \mu\text{sec}$;

(*) Sampling Rate $f_s = 10.24 \text{ MHz}$ Design Parameter

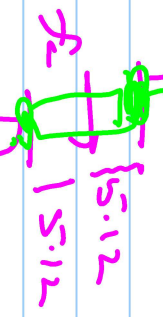
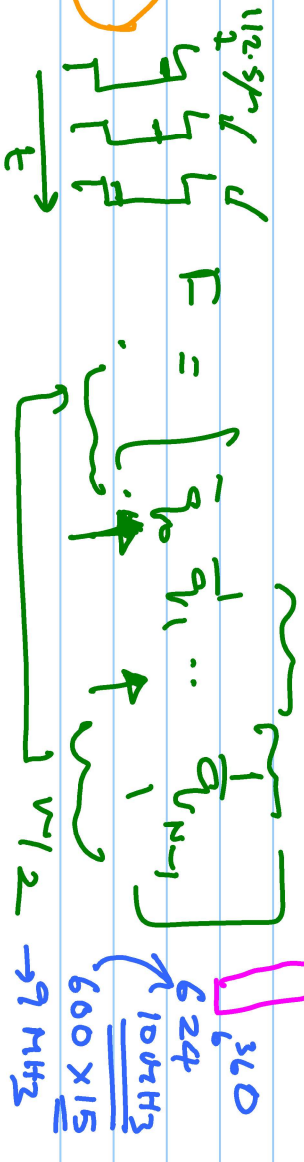
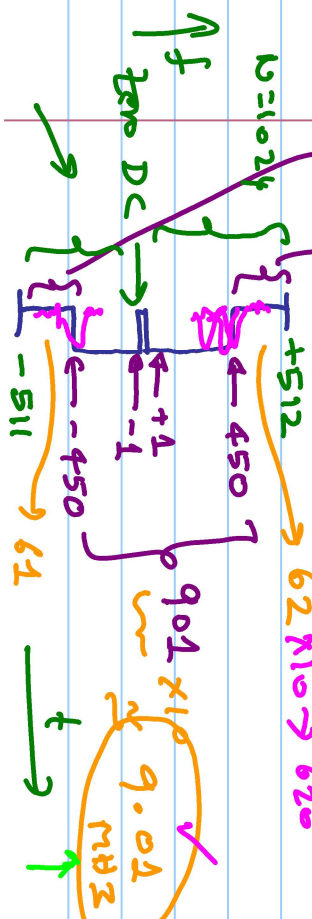
$T_{\text{ofDM}} = 112.5 \mu\text{s}$



$T_s = \frac{1}{10.24} \mu\text{sec}$
 $\Rightarrow 1024 \text{ samples} \rightarrow 100 \mu\text{sec}$

$N_{\text{sub}} = 128$, $N_u = 1024 = N$
 $N_{\text{ofDM}} = 1152 \text{ samples}$

Apparent $BW = 1024 \times 10 \text{ kHz} = 10.24 \text{ MHz}$



$1 \leq L \leq \frac{N_{CP}}{2}$

$N_{CP} \geq 2L$

$N_{CP}/2$

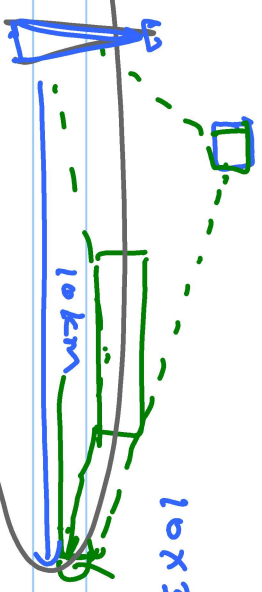
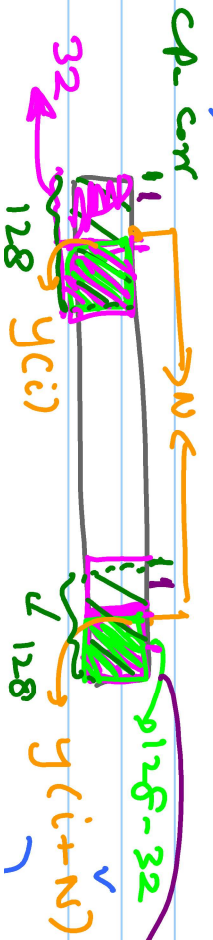
(worst case) Assume

$\Delta f = 17.6 \text{ kHz}$

Carrier Recovery

$f_c - f_c' = \Delta f$
 $\Delta f \text{ Doppler} \rightarrow 2v/\lambda = 0$

$L=1$
 No delay spread



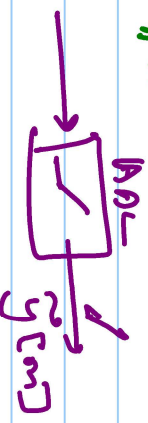
$10 \times 3.3 \mu s = 33 \mu s \ll 76 F$

20% → Delay spread

$12.5 \mu s$
 128

$6.6 \mu s$

with $p \neq p_k$ → tap $L \leq 64$



$Z(m) = \sum_{i=m-N_{CP}+1}^m y_c(i)$
 $L=1$

$$y(i) e^{-j2\pi \Delta f i T_s}$$

$$y(i+N) e^{-j2\pi \Delta f (i+N) T_s}$$

$$L = 32$$

$$M_{cp} = 128$$

$$z_c(i) = y(i) e^{-j2\pi \Delta f i T_s} \cdot y^*(i+N) e^{+j2\pi \Delta f (i+N) T_s} = |y(i)|^2 \cdot e^{j2\pi \Delta f N T_s}$$

$$\pm 2\pi \Delta f N \cdot T_s \leq \pm \pi$$

$$\Rightarrow 2 \cdot \Delta f \cdot N \cdot \frac{1}{\Delta f_{sub}} \leq 1$$

Check: $\Delta f = 17.6 \text{ kHz}$

$$N_s = 1024$$

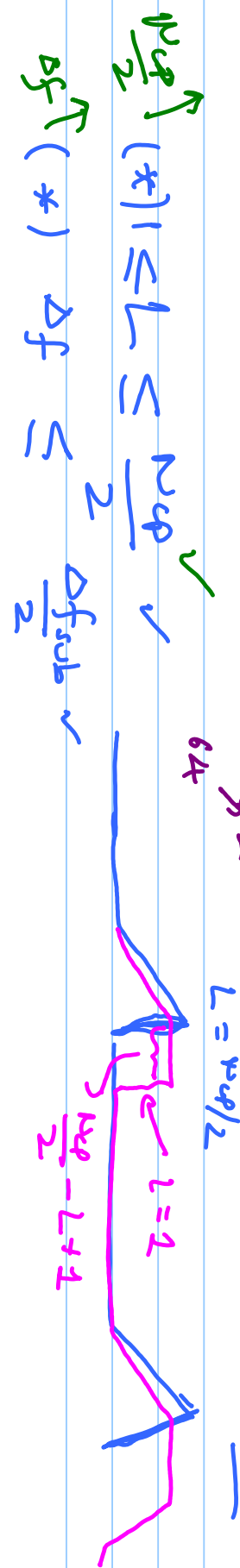
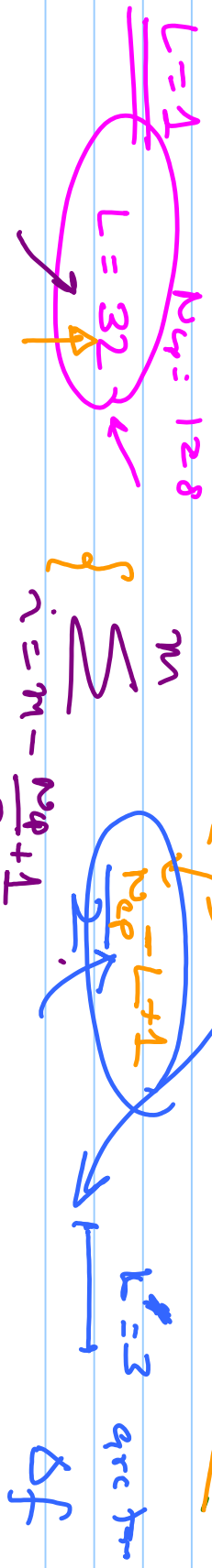
$$T_s = \frac{1}{10.24} \text{ } \mu\text{s} \approx 0.097 \mu\text{s}$$

$$\pm 2 \times 17.6 \times 10^3 \times 1024 \times \frac{1}{10.24} \times 10^{-6} \leq 1$$

$$2 \times 1.96 \times 10^3 \leq 1$$

$$T_s = \frac{1}{N \cdot \Delta f_{sub}}$$

$$\Delta f \leq \frac{\Delta f_{sub}}{2}$$



SNR → ?

$$y(m) = x(m) + v(m)$$

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$$|x_c|^2 + v^2$$

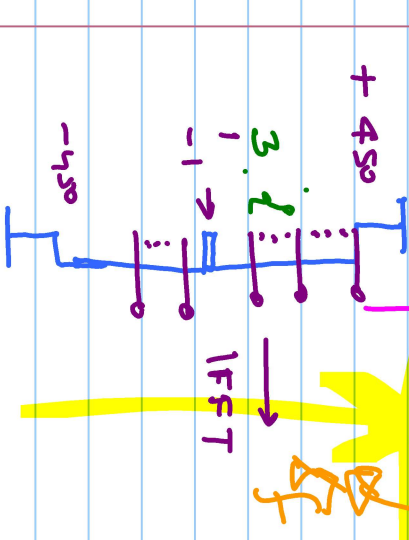
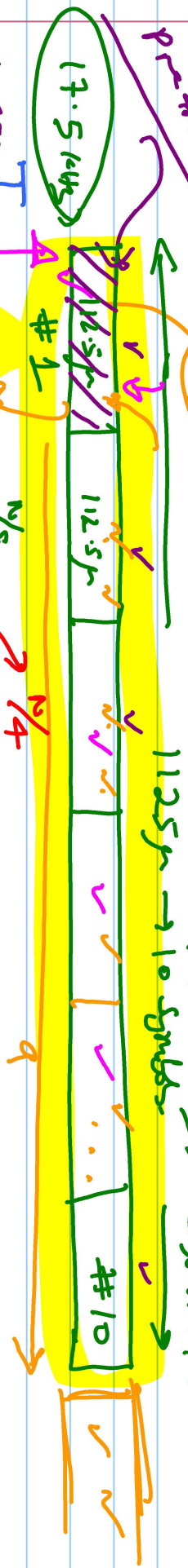
$$E[x(m)] = E[v(m)] = 0$$



BS

BS 100%

power spectral density



CFR

$$\Rightarrow \Delta f \leq 2 \Delta f_{sub}$$

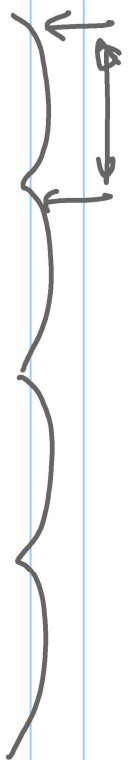
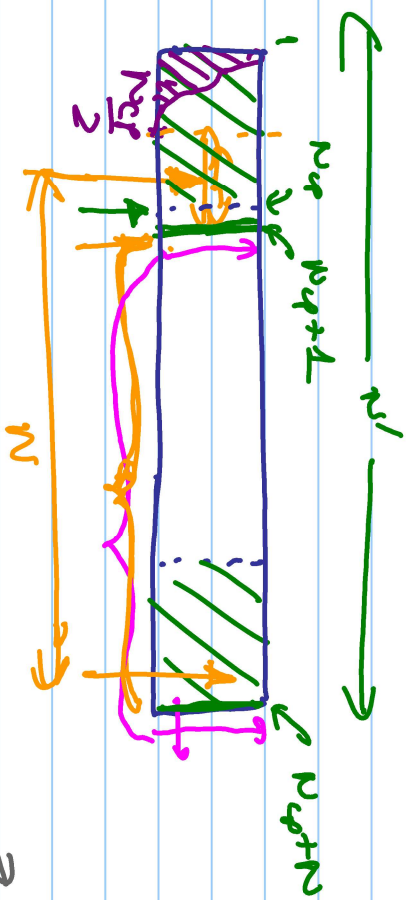
$$\Delta f \leq \pm \Delta f$$



$|Z(m)|$ Δf
 and $f_m(\cdot) \rightarrow \Delta f$
 $Z(m) =$

$$\sum_{i=m-N/4}^m y(i) y^*(i-N/4)$$

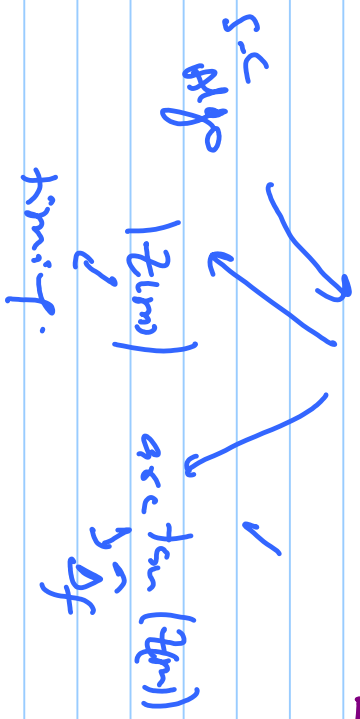
of copies $D = 4$
 $\Delta f \leq D \cdot \left(\frac{\Delta f_{sub}}{2} \right)$, $D = 1, 2, 4, 8, 16, \dots$
 $\left(\frac{3N}{4} \right)$



\rightarrow Schmidl & Cox

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$$z(m) = \sum_{i=m-\frac{N}{2}}^m y(i) y^*(i - \frac{N}{2})$$



$$\sum_{i=m-\frac{N}{2}}^m |y(i)|^2$$

L. Hanning ←

OFDM Channel Estimation → 2-4.30pm

