

**Tutorial Questions**

Note: Questions marked with “\*” are the harder ones; “\*\*” are beyond what was discussed in class; there are purely optional questions.

**1. Pilot Design and Overheads:** Consider a 20 MHz OFDM system with FFT size of  $N=1024$ . Assuming that the sub-carriers are indexed from 512 to -511, the guard sub-carriers are indexed by (512 to 472) and -472 to -511). The sampling rate is taken to be  $f_s = 20$  MHz. Answer now the following:

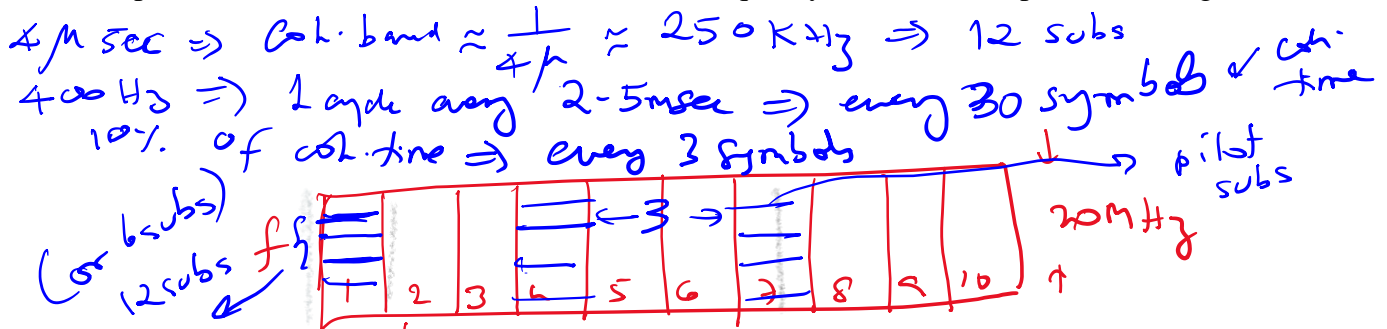
(a) What is the sub-carrier band-width  $\Delta f_{sub}$  in KHz? **Take 20MHz to be 20.48MHz for convenience!**

$$\Delta f_{sub} = 20.48 / 1024 = 20 \text{ KHz}$$

(b) If the Cyclic Prefix (CP) length  $N_{cp}$  is  $\frac{1}{4}$  of the useful symbol duration, what is the duration (in  $\mu\text{sec}$ ) of the full OFDM symbol?  $T_u = \frac{1}{\Delta f_{sub}} = \frac{1}{20 \text{ KHz}} = 50 \mu\text{sec}$ ;  $T_{cp} = \frac{50}{4} = 12.5 \mu\text{sec}$ ;  $T_{OFDM} = T_u + T_{cp} = 62.5 \mu\text{sec}$

(c) If QPSK modulation is employed on all the useful subcarriers, what is the “gross” spectral efficiency of this OFDM system (in bits/sec/Hz)?  $(471 \times 2) \times 2 \text{ bits/symbol} / 62.5 \mu\text{s} / 20.48 \text{ MHz}$   
 $\rightarrow 1.472 \text{ bits/Hz}$

(d) This system is deployed to cover a circular area of 3 km radius, where the delay spread is 4  $\mu\text{sec}$  or less. Also, the maximum Doppler frequency is expected to be 400Hz. Generally, it is advisable to have at least 1 or 2 pilot subcarriers (preferably 2 pilots) within a “Coherence band”, and pilots in time as often as every 10% of the “Coherence time” (which is approximately  $36^\circ$  phase change). Given this, how will you distribute pilot subcarriers in a 2-D manner (i.e., over frequency and time)? Explain with a figure.



(e)\* If 2ppm clocks are used on both the  $T_x$  and  $R_x$  nodes, how often should the preamble symbol be repeated in time so that between preambles, there is no more than half-a-sample of slip? (Hint: First find the slip-rate in number of sample slips per second.)

slip rate =  $(2+2) = 4 \text{ ppm} \times f_s \approx 20.48 \text{ MHz} \rightarrow$  taking 20 MHz  $\approx 80$  slips per sec  
 $\Rightarrow$  1 slip every  $\frac{1}{80} = 0.0122 \text{ sec} = 12.2 \text{ msec}$   
 $\Rightarrow$  preamble every  $12.2 \text{ msec} / 62.5 \mu\text{s} \approx 195$  symbols (blocks)

(f) Putting (d) and (e) together, make a neat sketch of the OFDM blocks, say drawn over two preamble intervals. The preamble can be assumed to also mark the beginning of a new frame. What is the frame rate in frames/sec?

(g) What is the “nett” spectral efficiency, after accounting for preamble and pilots?

multiply  $1.472 \times \left( \frac{194}{195} \right) \left( \frac{742 \times 3 - 742/12}{942 \times 3} \right)$  why?

(h) Now, the cell –radius is increased so that the maximum delay spread can at most equal the CP length defined in part (b). Recalculate your answer to part (d), and hence, redo your answer to part (g).

Do this!