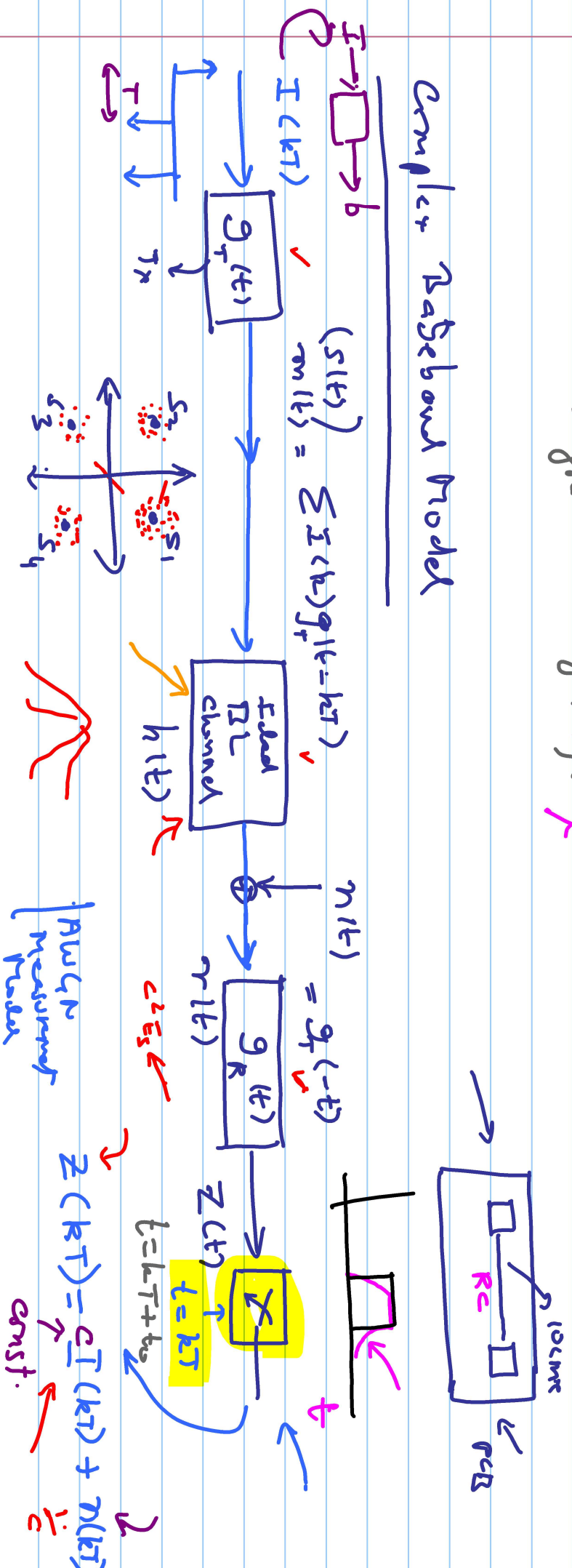


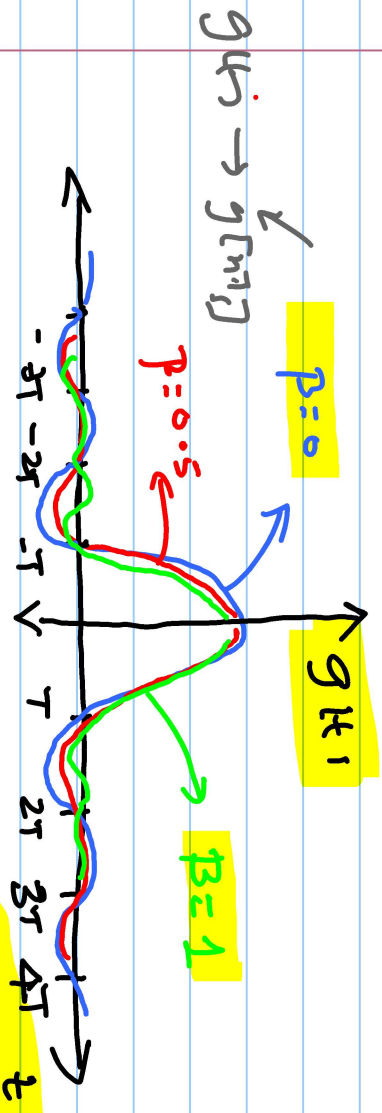
Signal Design for ~~Low~~ Band-limited Channels

Sampler Based Model

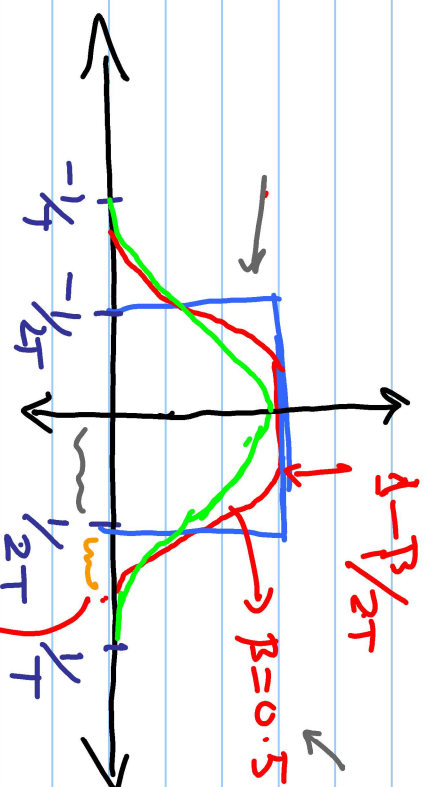


AWGN measurement model

Assume the use of Nyquist Pulse Shape $\begin{cases} \rightarrow \text{Sinc} \\ \rightarrow \text{Raised-Cosine} \end{cases}$



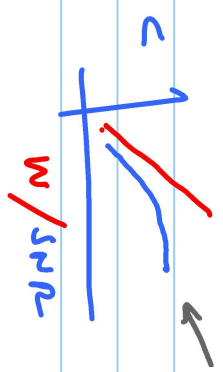
\Leftrightarrow

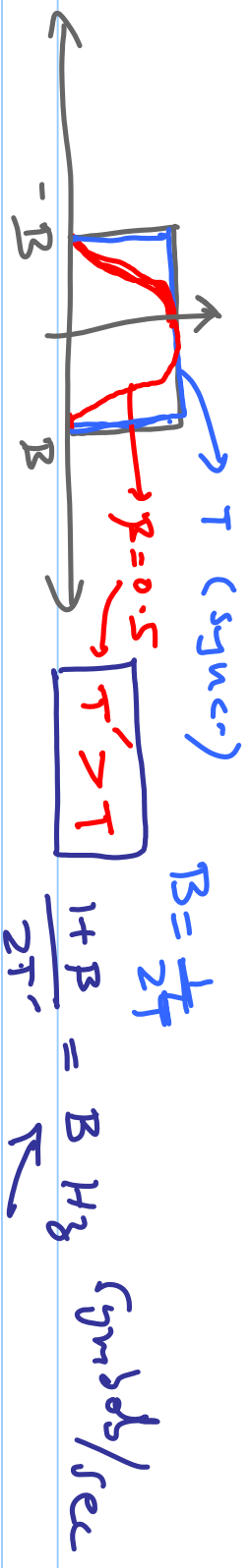


$$g_k(t) = \text{sinc}\left(\pi t / T\right) \cos\left(\frac{\pi \beta t / T}{1 - 4\beta^2 t^2 / T^2}\right)$$

$\beta \rightarrow$ excess BW factor

$\rightarrow C = \dot{W} \log_2(1 + \text{SNR})$





B → fixed,

$$\left\{ \begin{array}{l} \rightarrow R=0, \quad \frac{1}{2T} = B \\ \rightarrow R>0, \quad \frac{(1+R)}{2T'} = B \end{array} \right.$$

zero-ISI model

$$Z(z) = I(z) + n(z)$$

practical filter easier

(*) Timing error (due to incorrect sampling instant) is less
 (*) Rate loss since $T' > T$

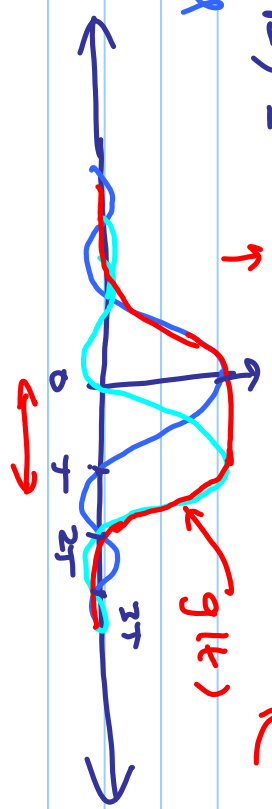
Q: Is it possible to not use excess BW & lose rate, and yet have readable filter?

A: yes → by introducing controlled ISI

eg: Duo-Binary Signal

$$z(k) = I(k) + I(k-1) + n(k)$$

Annotations: $z(k)$ (red), $I(k)$ (red), $I(k-1)$ (red), $n(k)$ (red)



$$z(k) - I(k-1) \approx y(k) = I(k) + n(k)$$

Annotations: $z(k)$ (purple), $I(k-1)$ (purple), $y(k)$ (green), $I(k)$ (purple), $n(k)$ (purple)

→ Preceding ✓

noises values

→ controlled IS

