

## EC-305 Communication Systems

Sept. 2009

Tutorial #2

KG / IITM

1. Referring to the Tutorial #2 of year 2008 (also enclosed), answer the following questions:

- (a) Framing: Problems 1,2, and 3
- (b) Switching: Problems 8,9,10, and 11
- (c) Erlang-B formula application: Problems 13 and 14

2. For the switch considered in Problem 8 (in tutorial #2 of year 2008), use the blocking probability expression following the work of Jacobaeus (which does not assume that the paths from input-to-middle stage and paths from output-to-middle stage are independent) given in eqn. (5.10) in page 239 of the book. What will be the new value of  $k$  for this case?

3. Consider a population of  $N=4000$  users, each of  $E_u=0.01$  Erlangs. Design a 3-stage blocking switch of least complexity such that the blocking probability  $P_b=10^{-4}$  or less. What is  $k$ , and the total number of cross-points for this switch? *Hint:* To minimize the total number of cross-points, choose the input sub-array dimension  $n$  “appropriately” where  $N/m=n$ .

4. Consider the 5-stage switch in the book, first described in page 237, Fig. 5.9. Here, blocking is introduced also in the middle stage(s). The input has  $N/n_1$  sub-arrays, each of dimension  $n_1 \times k_1$ , where  $N$  is the total population to be served by this switch. The middle-stage (which is actually a blocking switch with 3-stages) has  $k_1$  sub-arrays, each of size  $N/n_1 \times N/n_1$ . Each of these sub-arrays has  $N/(n_1 \times n_2)$  sub-arrays, of dimension  $n_2 \times k_2$  where  $k_2$  is the number of middle stage sub-arrays (each of dimension  $N/(n_1 \times n_2) \times N/(n_1 \times n_2)$ ). Assume each user offers  $E_u$  Erlangs of traffic.

(a) Prove using the Lee-Graph approach that blocking probability of the 5-stage switch is given by

$$P_b = \left\{ 1 - q_1^2 \left[ 1 - (1 - q_2^2)^{k_2} \right] \right\}^{k_1} \text{ where } q_1 = (1 - p_1) \text{ with } p_1 = \frac{n_1 E_u}{k_1} \text{ and } q_2 = (1 - p_2) \text{ with } p_2 = \frac{n_2 p_1}{k_2}.$$

(b) For  $N=50,000$ , and  $n_1=50$  and  $n_2=50$ , find the 5-stage switch with minimum number of cross-points so that  $P_b=10^{-8}$  or less. Assume  $E_u = 0.01$  Erlangs each.

(c) Can you find a better choice of  $n_1$  and  $n_2$  for this case? (i.e., a choice that will minimize the number of cross-points further?)

5. From “Digital Telephony” J.C.Bellamy, 3<sup>rd</sup> Ed., **Reading --** (a) Chapter 4: Framing in TDM; pp. 207 to 219, and (b) Chapter 5: Switching; pp. 225 to 261.