

Department of Electrical Engineering  
EC-305 Communication Systems

October 12, 2009

Quiz #2

20 marks

1. [3 marks] A framing code of length  $L_1=6$  is used on a frame of length  $N=100$ , to give an average frame acquisition time of  $S$  bits. Find the new value  $L_2$ , of this framing overhead that will reduce the average frame acquisition time to  $T$  bits, where  $T \leq \frac{S}{10}$ . What are the values of  $S$  and  $T$ ?

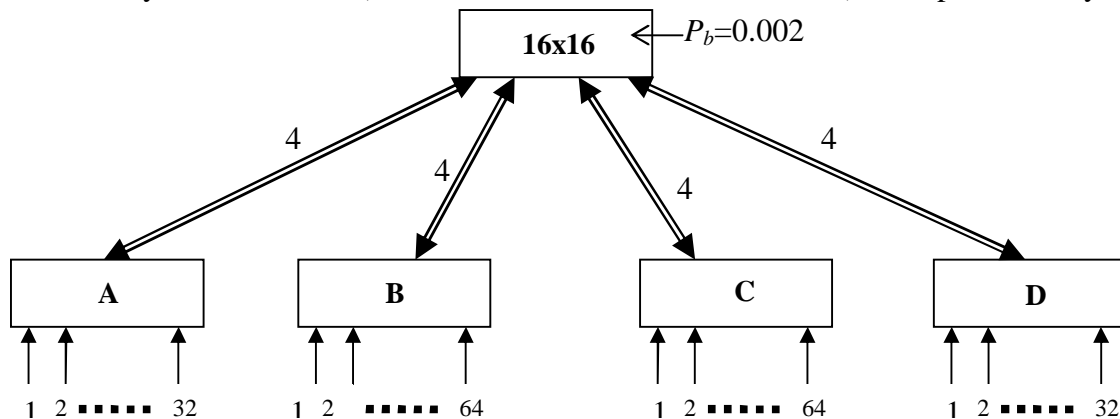
2. [3+4=7 marks] A particular synchronous link uses 100-bit long odd-numbered frames, and 50-bit long even numbered frames, as shown in figure below. The first bit in the 100-bit frame is always a “1” while the first bit is always “0” for the 50-bit frame. Framing is said to be achieved if over  $n=10$  consecutive frames, this framing bit sequence “1-0-1-0...” is correctly detected. Further, assume that some sort of scrambling-across-frames is done to ensure that in no (data) regular bit position will there be more than  $(n/2)-1=4$  consecutive “1”s or “0”s in as many consecutive frames (super-frames of length 150).



- (a) Describe a “parallel search” approach for framing detection. How many bit-locations are searched in parallel? How many bit intervals (assuming  $T$  is the bit-duration) elapse before framing is achieved?
- (b) Instead, for reasons of reducing complexity, if a “serial search” approach is taken, what will be:
  - (i) the best case, and (ii) the worst case situations (in terms of bit intervals required to achieve framing)?

3. [4 marks] Consider the design of a 3-stage blocking switch for  $N=10,000$  users, each offering  $E_u=0.02$  Erlangs. All the sub-arrays in the switch will be of dimension  $100 \times 100$  (and in the input and output stage sub-arrays, not all these links need to be used). Determine the (least) number of middle-stage subarrays,  $k$ , such that the blocking probability  $P_b$  is  $10^{-6}$  or lower. What is the total number of  $100 \times 100$  sub-arrays used in the switch?

4. [2+1+1+2=6 marks] We have 4 sub-switches A,B,C,&D, where the trunk traffic is served by 4 trunk lines each, as shown in the figure below. The trunk lines are in turn switched by a  $16 \times 16$  blocking switch with  $P_b=0.002$ . Assume that each of the trunk inlet ports (to A,B,C,&D) offer  $E_u=1/16$  Erlangs of traffic, and only the trunk-calls (i.e., calls to #s outside the sub-switch) are represented by the inlets.



- (a) Find the blocking probabilities (for connecting to the trunk servers) at sub-switch A and also at sub-switch B. (*Hint: use Erlang-B formula*)
- (b) What is the probability that a trunk user from switch A can connect to a trunk user in switch D?
- (c) What is the probability that a trunk user from switch A cannot connect to a user in switch C?
- (d) What is the overall average blocking probability of this switching trunk system?